# A Tale of Time Release powered by Blockchain and IBE

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\*Funded by an ERC grant

03.05.2025, Madrid



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two ways: Commit & Open Offline users?



Time Lock Puzzles Forced Opening possible!

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## Assumptions to build Time-Lock Puzzles



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## Assumptions to build Time-Lock Puzzles



Just use the blockchain as TTP.

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## PoS blockchain as TTP?



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#### Observations

- Trust infrastructure
- Periodic signing, Reference clock!
- $\blacktriangleright$   $\Rightarrow$  Reuse trust, committee work

## PoS blockchain as TTP?



#### Observations

- Trust infrastructure
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#### Goal: Off-Chain Tool

Public Enc- & Decryption

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- Minimize committee overhead!
- Concrete efficiency

## McFly - Verifiable Encryption to the Future Made Practical

Joint work of Nico Döttling<sup>1,\*</sup>, Lucjan Hanzlik<sup>1</sup>, Bernardo Magri<sup>2</sup> and Stella Wohnig<sup>1,3</sup> Published at Financial Crypto 2023 <sup>1</sup> Helmholtz Center for Information Security (CISPA) <sup>2</sup> The University of Manchester <sup>3</sup> Saarland University \* Funded by an ERC grant

## Vision



Previous work [LJKW18] How to build timelock encryption



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Our idea



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## Our idea

Time = block height. Users have read-only access to a blockchain.





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Signature Witness Encryption



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Signature Witness Encryption



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## t-of-n Signature Witness Encryption (basically)



ct = Enc(m, V, T)



 $m = Dec(ct, V, U, \sigma)$ 

Encrypt message m

- under potential signer set  $V = (vk_1, \dots, vk_n)$
- ► and reference message *T*

s.t. Decryption is possible iff we get indices I signatures  $\sigma_i, i \in I$ 

- ▶ s.t.  $\forall i \in I$  : Sig.Verify $(\sigma_i, T, \mathsf{vk}_i) = 1$
- and  $|I| \ge t$  (i.e.  $\ge t$  parties sign on T)

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## t-of-n Signature Witness Encryption (basically)



ct = Enc(m, V, T)



 $m = Dec(ct, V, U, \sigma)$ 

Security: IND-CPA

• For  $\leq t - 1$  dishonest keys

- and signing oracle for honest keys (Except for T\*)
- A chooses  $m_0, m_1$ , gets  $Enc(m_b, V, T^*)$ , guesses b

Encrypt message m

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## Blockchain assumptions

- Block production rate
- ► Honest majority ⇒ No premature signing



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Signature Witness Encryption

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 Choose signer set V as committee keys

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Availability of sig



## Blockchain assumptions

- Block production rate
- Honest majority
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- ► Known committee at decryption time ⇒ near-future



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# Signature Witness Encryption

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- Choose signer set V as committee keys
- Choose reference T as predictable block header of block T.



## Blockchain assumptions

- Block production rate
- Honest majority
  No premature signing
- ► Known committee at decryption time ⇒ near-future
- Custom block structure: Sign header seperately!



### Signature Witness Encryption

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#### $\mathsf{Claim:}\ \mathsf{IBE} \Rightarrow \mathsf{SWE}$

# $\label{eq:claim: IBE} \mathsf{SWE}$ $\blacktriangleright$ via the Naor transform we know: IBE $\Rightarrow$ Signatures

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- ▶ via the Naor transform we know:  $IBE \Rightarrow Signatures$
- this extends to:  $IBE \Rightarrow Signatures + SWE$

Given IBE

- $\blacktriangleright \mathsf{pk}, \mathsf{msk} \leftarrow \mathsf{Gen}(1^{\lambda})$
- $\blacktriangleright \mathsf{sk}_{\mathit{ID}} \leftarrow \mathsf{Ext}(\mathsf{msk}, \mathit{ID})$
- ▶ ct  $\leftarrow$  Enc(*m*, pk, *ID*)
- ▶  $m \leftarrow \text{Dec}(\text{sk}_{ID}, \text{ct}, \text{pk})$

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#### Construct Signature

- Gen: Output IBE.Gen
- Sign(M, msk):  $\sigma_M = sk_M$
- To verify Enc random message to ID M and see if decryption works

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Being able to decrypt is the same as being able to sign!
# SWE plausibility

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- ▶ pk, msk ← Gen $(1^{\lambda})$
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Construct Signature + 1-of-1 SWE

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- ► SWE.Enc(*m*, *V* = {pk}, *T*): IBE.Enc(*m*, pk, *ID* = *T*)
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For t-of-n add secret sharing

## Thresholdize

Assume we know a 1-of-1 SWE

• Thresholdizing it with multiplicative O(n) overhead



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#### Build for BLS signatures

- Deployed e.g. in Ethereum
- Efficient multi-signature

$$\mathbf{Q} \sigma_1 + \mathbf{Q} \sigma_3 = \mathbf{Q} \sigma_{1,3}$$

 Results from the Boneh-Franklin IBE via the Naor transform ⇒ 1-of-1 SWE for free

## BLS - Quick Recap

Let  $e : \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$  be a bilinear map, with Bilinear Diffie-Hellman assumption in  $(\mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T)$ , and H a hash function.

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#### **BLS Signature**

Key pairs:  $(sk \in \mathbb{Z}_p, vk = g_2^{sk})$ Sig $(sk, m) = H(m)^{sk}$ Verify $(vk, m, \sigma)$ : Output  $e(\sigma, g_2) \stackrel{?}{=} e(H(m), vk)$ 

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SWE (based on Boneh Franklin) Encrypt *m* to vk with reference *T*:  $c = g_2^r, c' = (e(H(T), vk))^r \cdot g_T^m$ Notice  $(e(H(T), vk))^r = e(\sigma, c)$ 

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### Multi Signature $Agg(\sigma_1, ..., \sigma_n) = \prod_{i \in [n]} \sigma_i$ AggVerify for m and $vk_1, ..., vk_n$ : $e(\sigma, g) \stackrel{?}{=}$ $\prod_{i \in [n]} e(H(m), vk_i)$

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Shamir's secret sharing: Split *m* into *n* shares  $s_1, \ldots, s_n$ s.t. for any  $\geq t$  shares we get  $m = \sum_j s_j L_j$ , for  $L_j$  Lagrange coefficients

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What about multi-signatures? Have:  $c'_i = g^{s_i} \cdot e(\sigma_i, g_2^r)$ , aggregated  $\sigma_I = \prod_{i \in I} \sigma_i$ 

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## Is that the time?!?!



- Build for BLS signatures
- Supports Multi-Signatures (at a price)

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  - supports commit & open, optimistic settings

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  - this is done by adding a Pederson commitment and a proof of plaintext equality

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Optimizes for concrete efficiency

Let's encrypt k messages, with n committee members:

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$$m_k \longrightarrow C_{k,0} C_{k,1} \dots C_{k,n} \longrightarrow g^{m_k}$$

 $m_k$ 

Let's encrypt k messages, with n committee members: Size  $O(n \cdot k)$ Enc Dec

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C<sub>k,0</sub> C<sub>k,1</sub>



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#### ▶ Batching: Size O(n + k)



- Batching: Size O(n+k)
- Packing: Allow m ∈ {0,...,2<sup>ℓ</sup> − 1} instead of bit messages (baby-step-giant-step)



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- ▶ Bilinear setup: e : G<sub>1</sub> × G<sub>2</sub> → G<sub>T</sub>. Group operations in G<sub>T</sub> usually most expensive. We move most operations into G<sub>2</sub>!

## Now what?

We built concretely efficient verifiable time release encryption

- from BDH and blockchain trust-assumptions
- with small overhead for committee
   (2 signatures per block + changed aggregation)
- for a limited time horizon.  $\rightarrow$  Future work!

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- [FMMMTV'22]: Cryptographic Oracle-based Conditional Payments
  - Similar primitive (VweTS)
  - Cool application: Construct blockchain payments conditioned on real-life events

Applications of SWE potentially see growing signer sets!

Asymptotics of O(n) in number of potential signers not ideal → Future work!

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- Similar IBE based construction for BLS
- Found perfect deployment environment: drand relatively fixed committee regularly signs predictable messages

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Runs in production, with a cute GUI webapp



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Highly permissioned system



# Maybe this is enough for your application and you can tune out now :)





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## Now what?

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But a theorist might want:

- Long-Term Encryption across Committees
- Better asymptotics without joint key setup

Long-Term encryption across committees?

Solved if we allow the committee to be more involved Solutions with near-future solution + bootstrapping to far-future by auxiliary committees

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Simple example: [BGGHKLRR20] - Can a public blockchain keep a secret?



To my knowledge no "off-chain" solution known to extend a time release among multiple committees

 $\Rightarrow$  YOUR future work?

# Signature-based Witness Encryption with Compact Ciphertext

Joint work of Gennaro Avitabile<sup>1</sup>, Nico Döttling<sup>2,\*</sup>, Bernardo Magri<sup>3</sup>, Christos Sakkas<sup>3</sup>, Stella Wohnig<sup>2,4</sup> Published at Asiacrypt 2024 <sup>1</sup> IMDEA Software Institute <sup>2</sup> CISPA Helmholtz Center for Information Security <sup>3</sup> The University of Manchester <sup>4</sup> Saarland University \* Funded by an ERC grant

#### High-level Overview so far

- Assume we know a 1-of-1 SWE (BF-IBE in BLS case)
- Thresholdizing it with multiplicative O(n) overhead



Batching via Symmetric Encryption

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How CAN we do better?

#### *iO* to the rescue



#### iO to the rescue

#### The superpower: replace circuits

 puncture a key to forget a value



Together they help forgetting a value in a circuit!



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#### High-level idea



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#### High-level idea



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Let a circuit create the shares.

## High-level idea



Let a circuit create the shares.

Circuit gets  $(i, vk_i, \sigma_i)$ , if valid returns share  $s_i$  (pulled from PPRF) This is O(polylog n).

Fully non-adaptive: reference T, corrupted parties known, all keys honestly created Want: Forget all honest shares, use secret sharing security.

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Intuition: Honest signatures are never given to  $\mathcal{A}$  so the circuit is never queried successfully to output honest share.

Puncture all honest keys



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#### Comparison



Concrete efficiency?

- BLS based construction
- Size O(n)
- Based on BDH, ROM

SWE, [DHMW'22]

#### Asymptotic efficiency?

- Generic construction
- Size O(polylog n)
- Uses iO

cSWE, [ADMSW'24]

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#### Future work

- Are there less heavy compact constructions?
- Find a bootstrapping to the far-future for McFly with no committee communication/joint key setup?
- Any chance if reference messages are not (fully) known?